

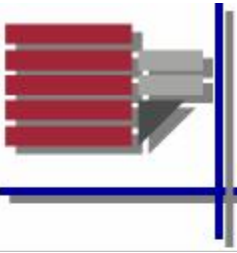
PRO-VE'10

11th IFIP Working Conference on VIRTUAL ENTERPRISES  
*Saint-Etienne, France, 11-13 October 2010*



***Eigenvector centrality  
based on shared research topics  
in a scientific community***

***Antonio P. Volpentesta, Alberto M. Felicetti***



# About us



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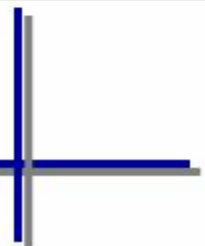


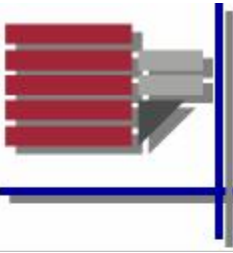
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GIUDALab:  
a lab of economics and management engineering  
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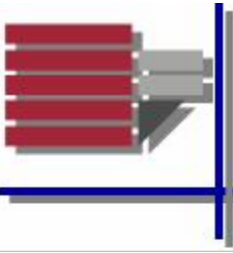




# Outline



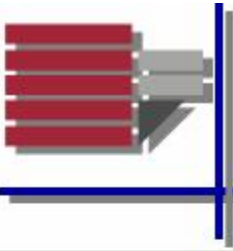
- *Introduction and Theoretical Background*
- *Eigenvector centrality for weighted multi-hypergraphs*
- *The weighted multi-hypergraph model*
- *A model instantiation for the Pro-VE community*
- *Conclusions and future works*



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# Introduction



## *Scientific Community (SC):*

Networks of scientists, researchers and professionals who aim to produce, in a collaborative way, new knowledge within a specific domain or issue-area.

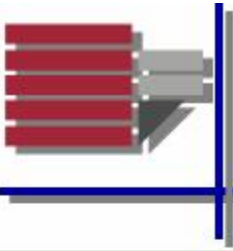
Key Factor for Scientific  
Knowledge development



***COLLABORATION***

## *ISSUE:*

**Scholars are often not aware of other researchers who are working on similar projects and have same interests**



# Introduction



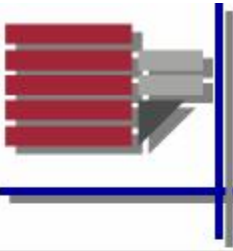
- Identify researchers who work on the same research topic.
- Highlight the *“importance”* of the different research topics (RTs) within a scientific community (SC).

*What does it mean “importance”?*

Relevance of a RT in a SC.

*How do we can quantify “importance”?*

By analyzing Centrality in a collaboration network of scientists.



# What is centrality?



***Network centrality:*** importance of a position within a network.

Idea of centrality comes from social networks literature.

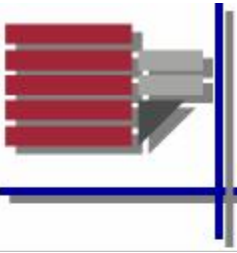
Multiple meanings of centrality:

***Degree centrality:*** Number of links incident upon a node.

***Closeness centrality:*** Nodes are more central if they can reach other nodes 'easily.'

***Betweenness centrality:*** Based on shortest paths in a network.

***Eigenvector centrality:*** Important nodes have important "friends"



# Introduction



## *Previous studies:*

Based primarily on graph structures.

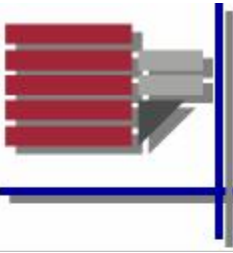
Few attempts in utilizing hypergraph in social network modeling.

## *What we propose:*

Model based on weighted multi-hypergraph to represent relationship between researchers and research interests.

Measure of the importance in a such network, by extending eigenvector centrality notion to a weighted multi-hypergraph.

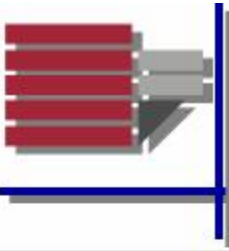




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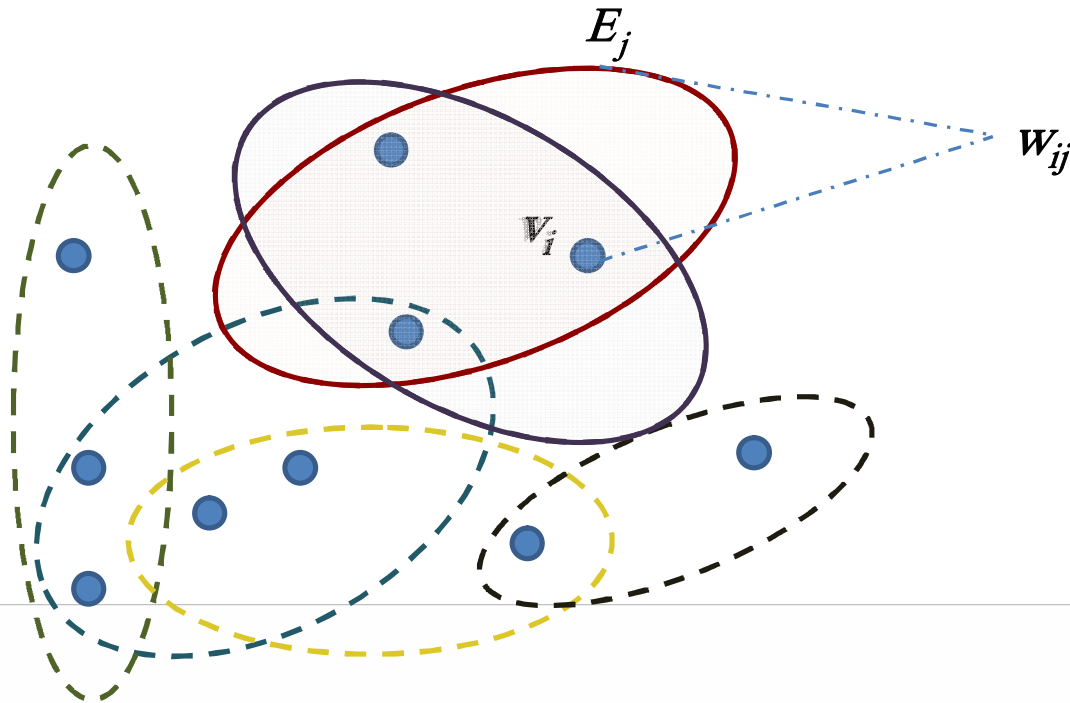
# The weighted multi-hypergraph model

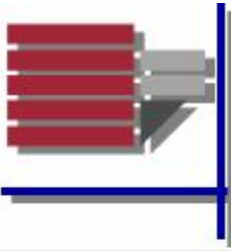


$\mathcal{H} (\mathcal{V}, \mathcal{E})$

$\mathcal{V} = \{v_1, \dots, v_m\}$  is a set of vertices.

$\mathcal{E} = \{E_1, \dots, E_n\}$  is a multi-set of nonempty subsets of  $\mathcal{V}$ , called hyperedges.





# Eigenvector centrality for weighted multi-hypergraphs



***Mutually reinforcing relationship*** assumption:

*An important hyperedge is a hyperedge whose elements are important vertices;  
An important vertex is a vertex that belongs to many important hyperedges.*

Numerically:

$x_i \rightarrow$  'importance' of vertex  $v_i$

$$x_i = c_1 \sum_{j=1}^n w_{ij} y_j, \quad \text{for } i = 1, \dots, m.$$

$y_j \rightarrow$  'importance' of hyperedge  $E_j$

$$y_j = c_2 \sum_{i=1}^m w_{ij} x_i, \quad \text{for } j = 1, \dots, n.$$

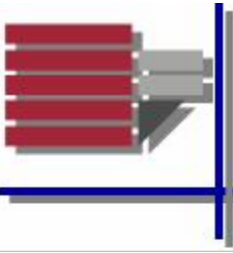
In matrix notation with  $\mathbf{x} = (x_1, x_2, \dots, x_m)$  and  $\mathbf{y} = (y_1, y_2, \dots, y_n)$  this yields:

$$\mathbf{W}\mathbf{W}^t\mathbf{x} = \lambda\mathbf{x},$$

$$\mathbf{W}^t\mathbf{W}\mathbf{y} = \lambda\mathbf{y},$$

where  $\lambda = c_1 c_2$ .

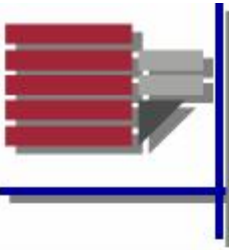
A solution is given by setting  $\lambda = \lambda^*$ , the dominant  $\mathbf{W}^t\mathbf{W}$ 's eigenvalue



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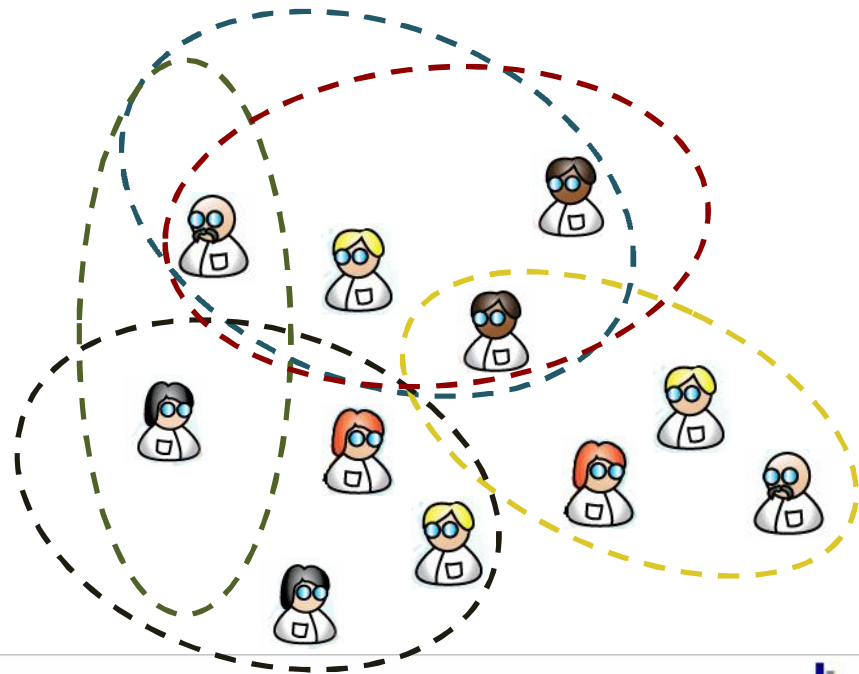
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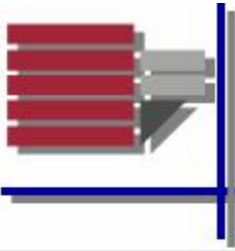


- $\mathbf{T} = \{t_1, \dots, t_m\}$  an ordered set of research interests (research topics);
- $\mathbf{R} = \{r_1, \dots, r_n\}$  an ordered set of researchers (authors), members of a SC;

Multi-hypergraph  $\mathcal{H} (\mathcal{R}, \mathcal{E})$

- $\mathcal{R} = \mathbf{R} = \{r_1, \dots, r_n\}$ ;
- $\mathcal{E} = \{E_1, \dots, E_m\}$ , with  $E_j = E(t_j)$





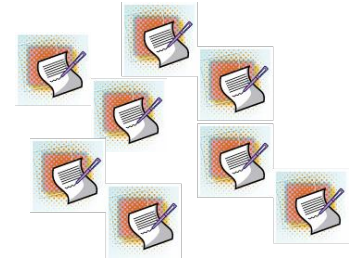
# The weighted multi-hypergraph model



*How to identify the research topics?*

*How to relate researcher to research topics?*

•  $\mathbf{D} = \{d_1, \dots, d_p\}$  an ordered set of documents (scientific papers);

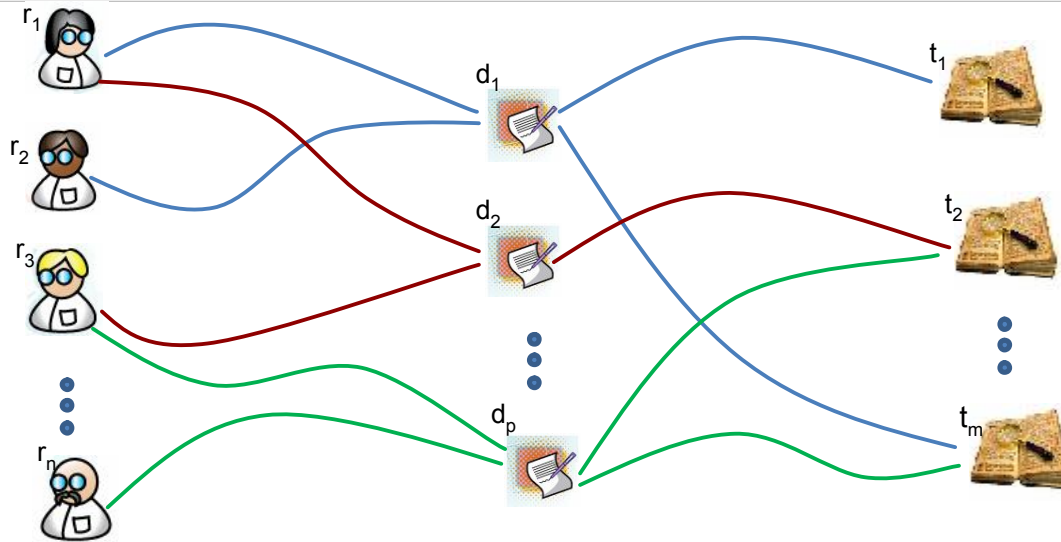


## Assumptions:

Research interests of any researcher  $r_i$  are manifested on documents whose  $r_i$  is an author;

The relationship between researchers and interest groups may be derived through a semantic analysis of the documents' content.

# The weighted multi-hypergraph model



- $A \in \mathbb{R}^{n \times p}$  a binary matrix that represents the relationships between authors and documents produced by them.
- $B \in \mathbb{R}^{p \times m}$  a nonnegative matrix that gives a measure of how much documents are devoted to research topics.
- $C = (c_1, c_2, \dots, c_p)$  a positive vector, where the generic entry  $c_k$  represents a measure of the popularity of  $d_k$  in the scientific community.



# The weighted multi-hypergraph model



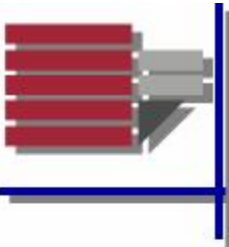
## Assumptions:

- The content of a document is due in equal measure to all its authors:  $a_{ik}/h_k$  ( $h_k$ , # of authors of  $d_k$ ) measures the document portion that is attributed to  $r_i$
- The number  $b_{kj} \cdot c_k$  measures the contribution given by the research topic  $t_j$  to the popularity of the document  $d_k$
- The number  $(a_{ik}/h_k) \cdot (b_{kj} \cdot c_k)$  measures the contribution given by the portion of  $d_k$  dealing with  $t_j$  and attributed to  $r_i$  to the popularity of  $d_k$

According to these assumptions and settings, we propose to estimate the weight associated to the couple  $(r_i, t_j)$ , as follows:

$$w_{ij} = \sum_{k=1}^p (a_{ik} / h_k) \cdot (b_{kj} \cdot c_k)$$





# The weighted multi-hypergraph model



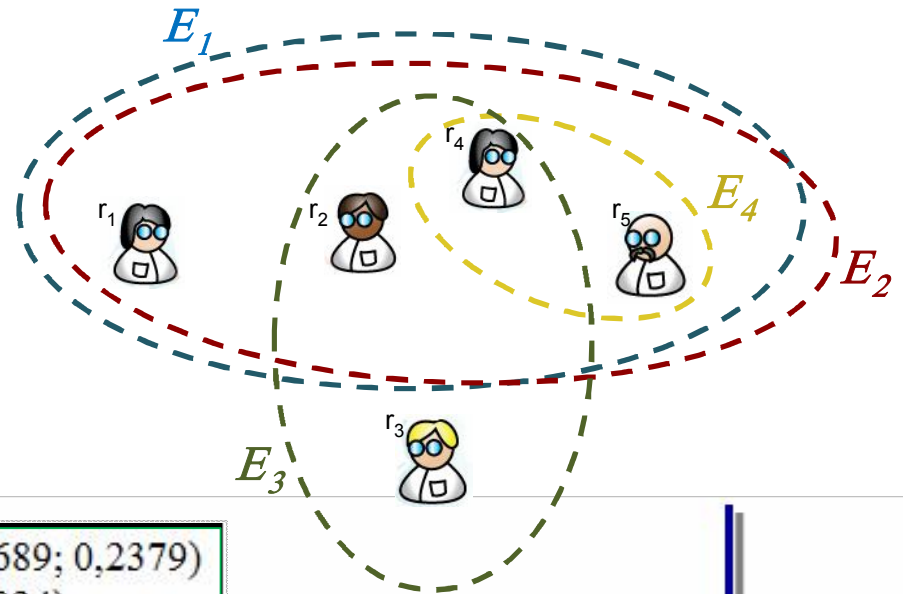
- $D = \{d_1, d_2, d_3\}$ ;  $T = \{t_1, t_2, t_3, t_4\}$ ;  $R = \{r_1, r_2, r_3, r_4, r_5\}$ ;  $C = (1, 2, 3)$ ;

A	$d_1$	$d_2$	$d_3$	B	$t_1$	$t_2$	$t_3$	$t_4$
$r_1$	1	0	0	$d_1$	3/4	1/4	0	0
$r_2$	1	1	0	$d_2$	0	0	1	0
$r_3$	0	1	0	$d_3$	1/4	1/4	0	1/2
$r_4$	0	1	1					
$r_5$	0	0	1					

$$h_k = \frac{1}{\sum_i a_{ik}} \quad k=1,2,3,$$

i.e.  $(h_1, h_2, h_3) = (2, 3, 2)$ ;

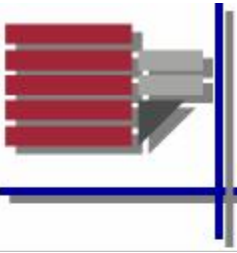
W	$t_1$	$t_2$	$t_3$	$t_4$
$r_1$	3/8	1/8	0	0
$r_2$	3/8	1/8	2/3	0
$r_3$	0	0	2/3	0
$r_4$	3/8	3/8	2/3	3/4
$r_5$	3/8	3/8	0	3/4



Results:

$$x = (0,0656; 0,1966; 0,1309; 0,3689; 0,2379)$$

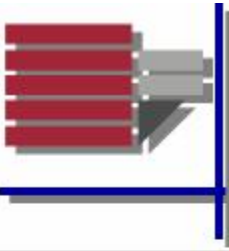
$$y = (0,2165; 0,1729; 0,3082; 0,3024)$$



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# *A model instantiation for the Pro-VE community*



- **D:** all selected papers that were published in the books of the last five Pro-Ve conferences (2005-2009);
- **R:** researchers who appeared as an author of at least one scientific article published in such books
- **A** represents relation between authorship and Pro-Ve papers.

## *What is a Research Topic (RT) in the Pro-Ve community?*

We have modeled a research topic in the triple (OF, DA, ES) , where:

- OF is the set of Collaborative Network (CN) Organizational Forms.
- DA is the set of Dimensional Aspects (Derived from ARCON Model) of a CN.
- ES is the set of the economic sectors, each one encompassing real business environments, where CN principles are instantiated and implemented.

**In other words, a RT is characterized by a dimensional aspect of a CN organizational form and possibly a case study or an application in primary industry, manufacturing, industrial services or intellectual services**



# A Research Topic in the Pro-VE community



## Dimensional Aspects

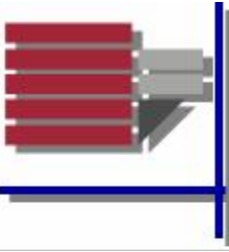
<b>Structural dimension</b>	Actors / relationships
	Roles
<b>Componential dimension</b>	Hardware / software resources
	Human resources
	Information / knowledge resources
	Ontology resources
<b>Functional dimension</b>	Processes
	Auxiliary processes
	Methodologies
<b>Behavioral dimension</b>	Prescriptive behavior
	Obligatory behavior
	Constraints and conditions
	Contracts and cooperation agreements
<b>Meta dimension</b>	
<b>External view</b>	

## CN Organisational Forms

<b>CN</b>	<b>Continuous production driven Network</b>	Supply chain
		Virtual Government
	<b>Market Opportunity driven Network</b>	Virtual Enterprise
		Virtual Organization
		Extended Enterprise
	<b>Human breeding environments (Communities)</b>	Virtual Team
		User's Community
		Community of Practices
	<b>Organizational breeding environments</b>	Industry Cluster
		Industrial District
Business Ecosystem		
Collaborative Virtual Lab		
		Disaster rescue Net

## Economic Sector

<b>Primary Economic Sector</b>	(i.e.): Agriculture, Fishing, Forestry, etc...
<b>Secondary Economic Sector</b>	(i.e.): Automotive, Construction, Electronics, Mechanical, Textile, etc
<b>Tertiary Economic Sector</b>	(i.e.): Industrial Services, Commerce, Transportation, Hospitality, Maintenance, etc..
<b>Quaternary Economic Sector</b>	(i.e.): Banking, Consulting, Education, Government Services, Healthcare, etc...
<b>No real world application</b>	



# *A model instantiation for the Pro-VE community*



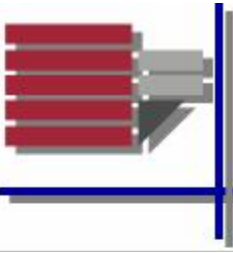
- **Matrix B:**

Obtained through a collaborative process of semantic analysis of Pro-VE papers;

- **Process** → Associate one or more instantiations of *(OF, DA, ES)* to any Pro-VE paper.

- **Assumptions**

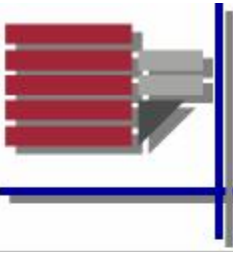
- Equi-distribution of the content of a paper among its research topics.
- Any entry  $c_k$  is instantiated at  $x_k + 1$  ( $x_k$ : number of documents in D that cite  $d_k$ )



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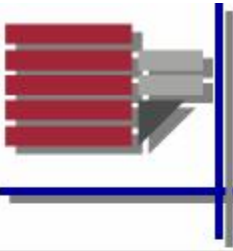
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# *Conclusions*



- We have proposed a model based on a weighted multi-hypergraph to represent relationships between researchers and research interests, grouping researchers with common interests.
- In order to measure the importance of researchers and research topics in a scientific community, we have extended the eigenvector centrality notion to this general logical structure and we present an algorithmic approach.
- We have described a first application of the model to the Pro-VE Community.

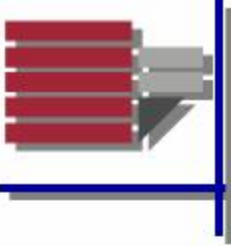


## *Further developments*



- Complete the implementation phase (we are collecting and validating data derived from a semantic analysis of Pro-Ve papers).
- Provide measurements and statistical analysis of the centrality of researcher and research topics within the Pro-Ve community.
- Extend this studies in order to map competences in a SC.
- Provide a competence map of the Pro-VE community.





*Thanks for your attention*

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